## FRACTIONS INCLUDING DECIMALS AND PERCENTAGES: PROGRESSION MAP FOR FLUENCY, REASONING AND PROBLEM SOLVING

Fractions including Decimals and Percentages: Statutory Requirements and Reasoning (from NCETM)

| COUNTING IN FRACTIONAL STEPS |  |  |  |  |  |
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| Year 1 | Year 2 | Year 3 | Year 4 | Year 5 | Year 6 |
|  | Pupils should count in fractions up to 10 , starting from any number and using the $1 / 2$ and $2 / 4$ equivalence on the number line (Non Statutory Guidance) | count up and down in tenths | count up and down in hundredths |  |  |
|  | Spot the mistake <br> 7, $7 \frac{1}{2}, 8,9,10$ <br> $8 \frac{1}{2}, 8,7,6 \frac{1}{2}$, <br> and correct it <br> What comes next? <br> $5 \frac{1}{2}, 6 \frac{1}{2}, 7 \frac{1}{2}$ <br> 9 $\frac{1}{2}, 9,8 \frac{1}{2}$, | Spot the mistake six tenths, seven tenths, eight tenths, nine tenths, eleven tenths and correct it. <br> What comes next? $\begin{aligned} & \text { 6/10, 7/10, 8/10, ....., .... } \\ & \text { 12/10, 11/10, ....., ....., ..... } \end{aligned}$ | Spot the mistake <br> sixty tenths, seventy tenths, eighty tenths, ninety tenths, twenty tenths ... and correct it. <br> What comes next? 83/100, 82/100, 81/100, ....., ....., ..... $31 / 100,41 / 100,51 / 100, \ldots . . .$ | Spot the mistake $0.088,0.089,1.0$ <br> What comes next? <br> $1.173,1.183,1.193$ | Spot the mistake <br> Identify and explain mistakes when counting in more complex fractional steps |


| RECOGNISING FRACTIONS |  |  |  |  |  |
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| Year 1 | Year 2 | Year 3 | Year 4 | Year 5 | Year 6 |
| recognise, find and name a half as one of two equal parts of an object, shape or quantity | recognise, find, name and write fractions ${ }^{1} / 3^{\prime}{ }^{1} / 4_{4^{\prime}}{ }^{2} /{ }_{4}$ and ${ }^{3} / 4$ of a length, shape, set of objects or quantity | recognise, find and write fractions of a discrete set of objects: unit fractions and non-unit fractions with small denominators <br> recognise that tenths arise from dividing an object into 10 equal parts and in dividing one-digit numbers or quantities by 10 . | recognise that hundredths arise when dividing an object by one hundred and dividing tenths by ten | recognise and use thousandths and relate them to tenths, hundredths and decimal equivalents (appears also in Equivalence) |  |
| recognise, find and name a quarter as one of four equal parts of an object, shape or quantity |  | recognise and use fractions as numbers: unit fractions and non-unit fractions with small denominators |  |  |  |
| What do you notice? <br> Choose a number of counters. Place them onto 2 plates so that there is the same number on each half. When can you do this and when can't you? What do you notice? | What do you notice? $\begin{aligned} & \frac{1}{4} \text { of } 4=1 \\ & \frac{1}{4} \text { of } 8=2 \\ & \frac{1}{4} \text { of } 12=3 \end{aligned}$ <br> Continue the pattern What do you notice? | What do you notice? $\begin{aligned} & 1 / 10 \text { of } 10=1 \\ & 2 / 10 \text { of } 10=2 \\ & 3 / 10 \text { of } 10=3 \end{aligned}$ <br> Continue the pattern. What do you notice? <br> What about $1 / 10$ of 20 ? Use this to work out 2/10 of 20, etc. | What do you notice? $\begin{aligned} & 1 / 10 \text { of } 100=10 \\ & 1 / 100 \text { of } 100=1 \\ & 2 / 10 \text { of } 100=20 \\ & 2 / 100 \text { of } 100=2 \end{aligned}$ <br> How can you use this to work out $6 / 10$ of 200? $6 / 100$ of 200 ? | What do you notice? <br> One tenth of £41 <br> One hundredth of $£ 41$ <br> One thousandth of £41 <br> Continue the pattern What do you notice? $\begin{aligned} & 0.085+0.015=0.1 \\ & 0.075+0.025=0.1 \\ & 0.065+0.035=0.1 \end{aligned}$ <br> Continue the pattern for the next five number sentences. | What do you notice? <br> One thousandth of my money is 31 p. How much do I have? |
| True or false? Sharing 8 apples between 4 children means each child has 1 apple. | True or false? <br> Half of $20 \mathrm{~cm}=5 \mathrm{~cm}$ <br> $\frac{3}{4}$ of $12 \mathrm{~cm}=9 \mathrm{~cm}$ | True or false? <br> $2 / 10$ of $20 \mathrm{~cm}=2 \mathrm{~cm}$ <br> $4 / 10$ of $40 \mathrm{~cm}=4 \mathrm{~cm}$ <br> $3 / 5$ of $20 \mathrm{~cm}=12 \mathrm{~cm}$ | True or false? <br> $1 / 20$ of a metre $=20 \mathrm{~cm}$ <br> $4 / 100$ of 2 metres $=40 \mathrm{~cm}$ | True or false? <br> 0.1 of a kilometre is 1 m . <br> 0.2 of 2 kilometres is 2 m . <br> 0.3 of 3 Kilometres is 3 m <br> 0.25 of 3 m is 500 cm . | True or false? $25 \%$ of 23 km is longer than 0.2 of 20 km . Convince me. |


|  |  |  |  | $2 / 5$ of $£ 2$ is 20 p |
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| COMPARING FRACTIONS |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Year 1 | Year 2 | Year 3 | Year 4 | Year 5 | Year 6 |
|  |  | compare and order unit fractions, and fractions with the same denominators |  | compare and order fractions whose denominators are all multiples of the same number | compare and order fractions, including fractions >1 |
|  |  | Give an example of a fraction that is less than a half. <br> Now another example that no one else will think of. Explain how you know the fraction is less than a half. (draw an image) <br> Ben put these fractions in order starting with the smallest. Are they in the correct order? <br> One fifth, one seventh, one sixth | Give an example of a fraction that is more than a half but less than a whole. <br> Now another example that no one else will think of. <br> Explain how you know the fraction is more than a half but less than a whole. (draw an image) | Give an example of a fraction that is more than three quarters. <br> Now another example that no one else will think of. Explain how you know the fraction is more than three quarters. <br> Imran put these fractions in order starting with the smallest. Are they in the correct order? <br> Two fifths, three tenths, four twentieths How do you know? | Give an example of a fraction that is greater than 1.1 and less than 1.5. Now another example that no one will think of. Explain how you know. <br> Sam put these fractions in order starting with the smallest. Are they in the correct order? <br> Thirty three fifths Twenty three thirds Forty five sevenths How do you know? |


| COMPARING DECIMALS |  |  |  |  |  |
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| Year 1 | Year 2 | Year 3 | Year 4 | Year 5 | Year 6 |
|  |  |  | compare numbers with the same number of decimal places up to two decimal places | read, write, order and compare numbers with up to three decimal places | identify the value of each digit in numbers given to three decimal places |
|  |  |  | Missing symbol <br> Put the correct symbol < or > in each box $\begin{array}{lll} 3.03 & \square .33 \\ 0.37 & \square & 0.32 \end{array}$ <br> What needs to be added to 3.23 to give 3.53 ? What needs to be added to 3.16 to give 3.2? | Missing symbol <br> Put the correct symbol < or > in each box <br> $4.627 \quad \square .06$ <br> $12.317 \quad \square \quad 12.31$ <br> What needs to be added to 3.63 to give 3.13? <br> What needs to be added to 4.652 to give 4.1? | True or false? <br> In all of the numbers below, the digit 6 is worth more than 6 hundredths. $$ <br> Is this true or false? Change some numbers so that it is true. <br> What needs to be adde3d to 6.543 to give 7 ? <br> What needs to be added to 3.582 to give 5 ? <br> Circle the two decimals which are closest in value to each other. $0.90 .090 .990 .10 .01$ |


| ROUNDING INCLUDING DECIMALS |  |  |  |  |
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| Year 1 | Year 2 | Year 3 | Year 4 | Year 6 |
|  |  | round decimals with one decimal place to the nearest whole number | round decimals with two decimal places to the nearest whole number and to one decimal place | solve problems which require answers to be rounded to specified degrees of accuracy |
|  |  | Do, then explain <br> Circle each decimal which when rounded to the nearest whole number is 5 . <br> $\begin{array}{llll}5.3 & 5.7 & 5.2 & 5.8\end{array}$ <br> Explain your reasoning <br> Top tips <br> Explain how to round numbers to one decimal place? <br> Also see rounding in place value | Do, then explain <br> Circle each decimal which when rounded to one decimal place is 6.2 . <br> $\begin{array}{llll}6.32 & 6.23 & 6.27 & 6.17\end{array}$ <br> Explain your reasoning <br> Top tips <br> Explain how to round decimal numbers to one decimal place? <br> Also see rounding in place value | Do, then explain <br> Write the answer of each calculation rounded to the nearest whole number $\begin{aligned} & 75.7 \times 59 \\ & 7734 \div 60 \\ & 772.4 \times 9.7 \\ & 20.34 \times(7.9-5.4) \end{aligned}$ <br> What's the same, what's different? <br> ... when you round numbers to one decimal place and two decimal places? <br> Also see rounding in place value |






|  |  |  |  |  | multiply one-digit numbers with up to two decimal places by whole numbers |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | find the effect of dividing a one- or two-digit number by 10 and 100 , identifying the value of the digits in the answer as ones, tenths and hundredths |  | multiply and divide numbers by 10,100 and 1000 where the answers are up to three decimal places |
|  |  |  |  |  | identify the value of each digit to three decimal places and multiply and divide numbers by 10,100 and 1000 where the answers are up to three decimal places |
|  |  |  |  |  | associate a fraction with division and calculate decimal fraction equivalents (e.g. 0.375) for a simple fraction (e.g. ${ }^{3 / 8}$ ) |
|  |  |  |  |  | use written division methods in cases where the answer has up to two decimal places |
|  |  |  | Undoing <br> I divide a number by 100 and the answer is 0.3 . What number did I start with? | Undoing <br> I divide a number by 100 and the answer is 0.33 What number did I start with? <br> Another and another Write down a number with two | Undoing <br> I multiply a number with three decimal places by a multiple of 10 . The answer is approximately 3.21 What was my number and what did I multiply buy? |


|  |  |  | Another and another <br> Write down a number with <br> one decimal place which <br> when multiplied by 10 gives <br> an answer between 120 and <br> 130. <br> $\ldots$ and another, ... and <br> another, ... | decimal places which when <br> multiplied by 100 gives an <br> answer between 33 and 38. <br> $\ldots$ and another, ... and <br> another, ... | When I divide a number by <br> 1000 the resulting number <br> has the digit 6 in the units <br> and tenths and the other <br> digits are 3 and 2 in the tens <br> and hundreds columns. What <br> could my number have been? |
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| PROBLEM SOLVING |  |  |  |  |  |
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| Year 1 | Year 2 | Year 3 | Year 4 | Year 5 | Year 6 |
|  |  | solve problems that involve all of the above | solve problems involving increasingly harder fractions to calculate quantities, and fractions to divide quantities, including non-unit fractions where the answer is a whole number | solve problems involving numbers up to three decimal places |  |
|  |  |  | solve simple measure and money problems involving fractions and decimals to two decimal places. | solve problems which require knowing percentage and decimal equivalents of ${ }^{1} /{ }_{2}$, ${ }^{1} / 4^{\prime}{ }^{1} / 5_{5^{\prime}}{ }^{\prime} /_{5^{\prime}}{ }^{4} /{ }_{5}$ and those with a denominator of a multiple of 10 or 25 . |  |

## Fractions including Decimals and Percentages: Key Performance Indicators

| Year 1 | Year 2 | Year 3 | Year 4 | Year 5 |
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|  |  |  | compare numbers with up to <br> 3 decimal places <br> Recognise \% symbol and <br> explain as a fraction with <br> denominator 100 (parts out <br> of 100) | between fractions, decimals <br> and percentages |
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Fractions including Decimals and Percentages: Cross-curricular links

| Year 1 | Year 2 | Year 3 | Year 4 | Year 5 | Year 6 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| DT - Cutting fruit in food technology to make a fruit kebab <br> Art - Making fruit collages | DT - making cakes using half ingredient |  |  | identify, name and write equivalent fractions of a given fraction, represented visually, including tenths and hundredths (Vikings and Anglo Saxons - designing a shield). |  |

## Fractions including Decimals and Percentages: Vocabulary

| Year 1 | Year 2 | Year 3 | Year 4 | Year 5 | Year 6 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Fraction <br> Equal part <br> Equal grouping <br> Equal sharing <br> One of two equal parts <br> One of four equal parts | Fraction <br> Equivalent fraction <br> Numerator <br> Denominator <br> Equal part <br> Equal grouping <br> Equal sharing <br> Parts of a whole <br> Half, two halves <br> One of two equal parts <br> Quarter, two .. three <br> One of four equal parts <br> One third <br> Two third <br> One of three equal parts | Fractions <br> Equivalent fraction <br> Numerator <br> Denominator <br> Half <br> Quarter <br> One third <br> Two third <br> Sixths/sevenths/eighths/tenths | fraction equivalent fraction mixed number numerator denominator equal part half quarter third sixths <br> sevenths eighths tenths hundredths decimal decimal fraction decimal point decimal place decimal equivalent | Fractions <br> Proper fraction <br> Improper fractions <br> Equivalent fractions <br> Mixed numbers <br> Numerator <br> Denominator <br> Equivalent <br> Reduced to <br> Cancel <br> Parts of a whole <br> Thousandths <br> Decimal/decimal fractions <br> Decimal point <br> Decimal place <br> Decimal equivalent <br> Proportion <br> In every <br> For every <br> Percentage <br> Per cent <br> \% | ```fraction proper/improper fraction equivalent fraction mixed number numerator denominator equivalent reduced to proportion in every for every ratio percentage per cent \%``` |

