# FRACTIONS INCLUDING DECIMALS AND PERCENTAGES: PROGRESSION MAP FOR FLUENCY, REASONING AND PROBLEM SOLVING

### Fractions including Decimals and Percentages: Statutory Requirements and Reasoning (from NCETM)

		COUNTING IN FR	ACTIONAL STEPS		
Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
	Pupils should count in	count up and down in tenths	count up and down in		
	fractions up to 10, starting		hundredths		
	from any number and using				
	the1/2 and 2/4 equivalence				
	on the number line (Non				
	Statutory Guidance)				
	Spot the mistake	Spot the mistake	Spot the mistake	Spot the mistake	Spot the mistake
	7, 7 <sup>1</sup> / <sub>2</sub> , 8, 9, 10	six tenths, seven tenths,			
	$8\frac{1}{2}, 8, 7, 6\frac{1}{2},$	eight tenths, nine tenths,	sixty tenths, seventy	0.088, 0.089, 1.0	Identify and explain
	and correct it	eleven tenths	tenths, eighty tenths, ninety		mistakes when counting in
	W/hat somes nout?	and correct it.	tenths, twenty tenths		more complex fractional
	What comes next?	What comes next?	and correct it.		steps
	$5\frac{1}{2}, 6\frac{1}{2}, 7\frac{1}{2},,$ $9\frac{1}{2}, 9, 8\frac{1}{2},,$	6/10, 7/10, 8/10,,	What comes next?	What comes next?	
	<i>y</i> <sub>2</sub> , <i>y</i> , <i>u</i> <sub>2</sub> ,,,	12/10, 11/10,,	83/100, 82/100, 81/100,,	1 172 1 102 1 102	
		12/10, 11/10,,,	837100, 827100, 817100,,	1.173, 1.183, 1.193	
			,		
			21/100 41/100 51/100		
			31/100, 41/100, 51/100,,		
			,		

## Fractions including Decimals and Percentages Progression Document

RECOGNISING FRACTIONS						
Year 1	Year 2	Year 3	Year 4	Year 5	Year 6	
recognise, find and name a half as one of two equal parts of an object, shape or quantity	recognise, find, name and write fractions $\frac{1}{3}, \frac{1}{4}, \frac{2}{4}$ and $\frac{3}{4}$ of a length, shape, set of objects or quantity	recognise, find and write fractions of a discrete set of objects: unit fractions and non-unit fractions with small denominators	recognise that hundredths arise when dividing an object by one hundred and dividing tenths by ten	recognise and use thousandths and relate them to tenths, hundredths and decimal equivalents (appears also in Equivalence)		
recognise, find and name a quarter as one of four equal parts of an object, shape or quantity		recognise that tenths arise from dividing an object into 10 equal parts and in dividing one - digit numbers or quantities by 10. recognise and use fractions as numbers: unit fractions and non-unit fractions with small denominators				
What do you notice? Choose a number of counters. Place them onto 2 plates so that there is the same number on each half. When can you do this and when can't you? What do you notice?	What do you notice? $\frac{1}{4}$ of 4 = 1 $\frac{1}{4}$ of 8 = 2 $\frac{1}{4}$ of 12 = 3 Continue the pattern What do you notice?	What do you notice? 1/10 of 10 = 1 2/10 of 10 = 2 3/10 of 10 = 3 Continue the pattern. What do you notice? What about 1/10 of 20? Use this to work out 2/10 of 20, etc.	What do you notice? 1/10 of 100 = 10 1/100 of 100 = 1 2/10 of 100 = 20 2/100 of 100 = 2 How can you use this to work out 6/10 of 200? 6/100 of 200?	What do you notice? One tenth of £41 One hundredth of £41 One thousandth of £41 Continue the pattern What do you notice? 0.085 + 0.015 = 0.1 0.075 + 0.025 = 0.1 0.065 + 0.035 = 0.1 Continue the pattern for the next five number sentences.	What do you notice? One thousandth of my money is 31p. How much do I have?	
<b>True or false?</b> Sharing 8 apples between 4 children means each child has 1 apple.	True or false? Half of 20cm = 5cm <sup>3</sup> / <sub>4</sub> of 12cm = 9cm	True or false? 2/10 of 20cm = 2cm 4/10 of 40cm = 4cm 3/5 of 20cm = 12cm	True or false? 1/20 of a metre= 20cm 4/100 of 2 metres = 40cm	True or false? 0.1 of a kilometre is 1m. 0.2 of 2 kilometres is 2m. 0.3 of 3 Kilometres is 3m 0.25 of 3m is 500cm.	True or false? 25% of 23km is longer than 0.2 of 20km. Convince me.	

	2/5 of £2 is 20p	

		COMPARING	FRACTIONS		
Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
		compare and order unit fractions, and fractions with the same denominators		compare and order fractions whose denominators are all multiples of the same number	compare and order fractions, including fractions >1
		Give an example of a fraction that is less than a half. Now another example that no one else will think of. Explain how you know the fraction is less than a half. (draw an image)	Give an example of a fraction that is more than a half but less than a whole. Now another example that no one else will think of.	Give an example of a fraction that is more than three quarters. Now another example that no one else will think of. Explain how you know the fraction is more than three quarters.	Give an example of a fraction that is greater than 1.1 and less than 1.5. Now another example that no one will think of. Explain how you know.
		Ben put these fractions in order starting with the smallest. Are they in the correct order? One fifth, one seventh, one sixth	Explain how you know the fraction is more than a half but less than a whole. (draw an image)	Imran put these fractions in order starting with the smallest. Are they in the correct order? Two fifths, three tenths, four twentieths How do you know?	Sam put these fractions in order starting with the smallest. Are they in the correct order? Thirty three fifths Twenty three thirds Forty five sevenths How do you know?

			COMPARING DECIMAL	5	
Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
			compare numbers with the	read, write, order and compare numbers	identify the value of each digit in
			same number of decimal places	with up to three decimal places	numbers given to three decimal
			up to two decimal places		places
			Missing symbol	Missing symbol	True or false?
			Put the correct symbol < or > in	Put the correct symbol < or > in each box	In all of the numbers below, the
			each box	4.627 4.06	digit 6 is worth <u>more than</u> 6
			3.03 3.33	-	hundredths.
			_	12.317 12.31	
			0.37 0.32		3.6 3.063 3.006
					6.23 7.761
					3.076
				What needs to be added to 3.63 to give	Is this true or false?
				3.13?	Change some numbers so that it
			What needs to be added to	What needs to be added to 4.652 to give	is true.
			3.23 to give 3.53? What needs to be added to	4.1?	What needs to be adde3d to
			3.16 to give 3.2?		6.543 to give 7?
			5.10 TO give 5.24		What needs to be added to
					3.582 to give 5?
					3.362 TO give 57
					Circle the two decimals which
					are closest in value to each
					are closest in value to each
					other. 0.9 0.09 0.99 0.1 0.01
					0.9 0.09 0.99 0.1 0.01

	ROUNDING INCLUDING DECIMALS							
Year 1	Уеа	ir 2	Year 3		Year 4	Year 5	Year 6	
			round decimals with one decimal place to the ne whole number <b>Do, then explain</b> Circle each decimal whi	arest	the nearest whole n decimal place Do, then explain	two decimal places to umber and to one which when rounded to	solve problems which require answers to be rounded to specified degrees of accuracy <b>Do, then explain</b> Write the answer of each	
			rounded to the nearest number is 5. 5.3 5.7 5.2 5.8 Explain your reasoning <b>Top tips</b> Explain how to round nu to one decimal place? Also see rounding in pla	whole umbers	one decimal place is 6.32 6.23 6.27 Explain your reasoni Top tips	6.2. 6.17 ng d decimal numbers to	calculation rounded to the nearest whole number 75.7 × 59 7734 ÷ 60 772.4 × 9.7 20.34 × (7.9 - 5.4) What's the same, what's different? when you round numbers to one decimal place and two decimal places? Also see rounding in place value	

	EQUIVALENCE (1	INCLUDING FRACTIONS, DECI	MALS AND PERCENTAGES)	
Year 1 Ye	ar 2	Year 3	Year 4 Year 5	Year 6
write simple fractions e.g. $\frac{1}{2}$ of 6 = 3 and recognise the equivalence of $\frac{2}{4}$ and $\frac{1}{2}$ .	recognise and show, using diagrams, equivalent fractions with small denominators	recognise and show, using diagrams, families of common equivalent fractions	identify, name and write equivalent fractions of a given fraction, represented visually, including tenths and hundredths	use common factors to simplify fractions; use common multiples to express fractions in the same denomination
Odd one out.Which is the odd one outin this trio: $\frac{1}{2}$ $\frac{1}{2}$ $2/4$ $\frac{1}{4}$ Why?What do you notice?Find $\frac{1}{2}$ of 8.Find 2/4 of 8What do you notice?	Odd one out.Which is the odd oneout in each of thesetrios $\frac{1}{2}$ $3/6$ $5/8$ $3/9$ $2/6$ $4/9$ Why?What do you notice?Find $2/5$ of 10Find $4/10$ of 10.What do you notice?Can you write anyother similarstatements?	Odd one out. Which is the odd one out in each of these trio $s_4^3$ 9/12 4/6 9/12 10/15 2/3 Why? What do you notice? Find 4/6 of 24 Find 2/3 of 24 What do you notice? Can you write any other similar statements?	Odd one out. Which is the odd one out in each of these collections of 4 fractions 6/10 3/5 18/20 9/15 30/100 3/10 6/20 3/9 Why? What do you notice? Find 30/100 of 200 Find 3/10 of 200 What do you notice? Can you write any other similar statements?	Odd one out. Which is the odd one out in each of these collections of 4 fraction $s_{4}^{3}$ 9/12 26/36 18/24 4/20 1/5 6/25 6/30 Why? What do you notice? 8/5 of 25 = 40 5/4 of 16 = 20 7/6 of 36 - 42 Can you write similar statements?
		recognise and write decimal equivalents of any number of tenths or hundredths	read and write decimal numbers as fractions (e.g. $0.71 = \frac{71}{100}$ ) recognise and use thousandths and relate them to tenths, hundredths and decimal equivalents	associate a fraction with division and calculate decimal fraction equivalents (e.g. 0.375) for a simple fraction (e.g. $\frac{3}{8}$ )
		Complete the pattern by	Complete the pattern	Complete the pattern
		filling in the blank cells in this table: $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$

		10       20       40         100       100       100         0.1       0.3       0.3         Another and another       Write a decimal numbers (to one decimal place) which lies between a half and three quarters?       and another, and another,	Complete the table. Another and another Write a fraction with a denominator of one hundred which has a value of more than 0.75? and another, and another,	Complete the table. Another and another Write a unit fraction which has a value of less than 0.5? and another, and another,
		recognise and write decimal equivalents to $\frac{1}{4}$ ; $\frac{1}{2}$ ; $\frac{3}{4}$	recognise the per cent symbol (%) and understand that per cent relates to "number of parts per hundred", and write percentages as a fraction with denominator 100 as a decimal fraction	recall and use equivalences between simple fractions, decimals and percentages, including in different contexts.
Ordering Put these fractions in the correct order, starting with the smallest. $\frac{1}{2}$ $\frac{1}{4}$ 1/3	Ordering Put these fractions in the correct order, starting with the smallest. $4/8 = \frac{3}{4} = 1/4$	OrderingPut these numbers in the correct order, starting with the smallest.↓↓0.755/10Explain your thinking	Ordering Put these numbers in the correct order, starting with the largest. 7/10, 0.73, 7/100, 0.073 71% Explain your thinking Which is more: 20% of 200 or 25% of 180? Explain your reasoning.	Ordering Which is larger, <sup>1</sup> / <sub>3</sub> or <sup>2</sup> / <sub>5</sub> ? Explain how you know. Put the following amounts in order, starting with the largest. 23%, 5/8, 3/5, 0.8

## Fractions including Decimals and Percentages Progression Document

## Charles Darwin Community Primary School

		ADDITION AND SUB	TRACTION OF FRACTIONS		
Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
		add and subtract fractions with the same denominator within one whole (e.g. $\frac{5}{7}$ , + $\frac{1}{7}$ , = $\frac{6}{7}$ )	add and subtract fractions with the same denominator	add and subtract fractions with the same denominator and multiples of the same number	add and subtract fractions with different denominators and mixed numbers, using the concept of equivalent
		, , , , , , , , , , , , , , , , , , ,		recognise mixed numbers and improper fractions and convert from one form to the other and write mathematical statements > 1	fractions
				as a mixed number (e.g. $^{2}/_{5}$ + $^{4}/_{5}$ = $^{6}/_{5}$ = $1^{1}/_{5}$ )	
		What do you notice?	What do you notice?	What do you notice?	Another and another Write down two fractions
		1/10 + 9/10 = 1	5/5 - 1/5 = 4/5	3/4 and 1/4 = 4/4 = 1	which have a difference of
		2/10 + 8/10 = 1	4/5 - 1/5 = 3/5	$4/4$ and $\frac{1}{4} = 5/4 = 1 \frac{1}{4}$	1 2/ and another, and
		3/10 + 7/10 = 1	Continue the pattern	$5/4$ and $\frac{1}{4} = 6/4 = 1\frac{1}{2}$	another,
		Continue the pattern		Continue the pattern up to the total of 2.	
			Can you make up a similar		Another and another
		Can you make up a similar pattern for eighths?	pattern for addition?	Can you make up a similar pattern for subtraction?	Write down 2 fractions with a total of 3 4/5.
			The answer is 3/5, what is		and another, and
		The answer is 5/10, what is the question? (involving	the question?	The answer is 1 2/5 , what is the question	another,
		fractions / operations)	What do you notice?		
			11/100 + 89/100 = 1		
			12/100 + 88/100 = 1		
			13/100 + 87/100 = 1		
			Continue the pattern for the		
			next five number sentences		

	MULTIPLICATION AND DIVISION OF FRACTIONS						
Year 1	Year 2	Year 3	Year 4	Year 5	Year 6		
				multiply proper fractions and mixed numbers by whole numbers, supported by materials and diagrams	multiply simple pairs of proper fractions, writing the answer in its simplest form $(e.g. \frac{1}{4} \times \frac{1}{2} = \frac{1}{8})$		
					multiply one-digit numbers with up to two decimal places by whole numbers		
					divide proper fractions by		
					whole numbers (e.g. $\frac{1}{3} \div 2 =$		
					<sup>1</sup> / <sub>6</sub> )		
				Continue the pattern	Continue the pattern		
					1/3 ÷ 2 = 1/6		
				$\frac{1}{4} \times 3 =$	1/6 ÷ 2 = 1/12		
				$\frac{1}{4} \times 4 =$ $\frac{1}{4} \times 5 =$	1/12 ÷ 2 = 1/24		
				₹ x 5 = Continue the pattern for			
				five more number sentences.	What do you notice?		
				How many steps will it take to get to 3?	$\frac{1}{2} \times \frac{1}{4} =$		
				5/3 of 24 = 40 Write a similar sentence where the answer is 56.	The answer is 1/8 , what is the question (involving fractions / operations)		
				The answer is 2 $\frac{1}{4}$ , what is the question	Give your top tips for dividing fractions.		
				Give your top tips for multiplying fractions.			

			multiply one-digit numbers with up to two decimal places by whole numbers
	find the effect of dividing a one- or two-digit number by 10 and 100, identifying the value of the digits in the answer as ones, tenths and hundredths		multiply and divide numbers by 10, 100 and 1000 where the answers are up to three decimal places
			identify the value of each digit to three decimal places and multiply and divide numbers by 10, 100 and 1000 where the answers are up to three decimal places
			associate a fraction with division and calculate decimal fraction equivalents (e.g. 0.375) for a simple fraction (e.g. <sup>3</sup> / <sub>8</sub> )
			use written division methods in cases where the answer has up to two decimal places
	Undoing I divide a number by 100 and the answer is 0.3. What number did I start with?	Undoing I divide a number by 100 and the answer is 0.33 What number did I start with? Another and another Write down a number with two	Undoing I multiply a number with three decimal places by a multiple of 10. The answer is approximately 3.21 What was my number and what did I multiply buy?

## Fractions including Decimals and Percentages Progression Document

	Anot	other and another	decimal places which when	When I divide a number by
			multiplied by 100 gives an	1000 the resulting number
	Writ	rite down a number with	answer between 33 and 38.	has the digit 6 in the units
	onec	e decimal place which	and another, and	and tenths and the other
	when	en multiplied by 10 gives	another,	digits are 3 and 2 in the tens
	an an	answer between 120 and		and hundreds columns. What
	130.	D.		could my number have been?
	and	and another, and		
	anoth	other,		

	PROBLEM SOLVING						
Year 1	Year 2	Year 3	Year 4	Year 5	Year 6		
		solve problems that involve all of the above	solve problems involving increasingly harder fractions to calculate quantities, and fractions to divide quantities, including non-unit fractions where the answer is a whole number	solve problems involving numbers up to three decimal places			
			solve simple measure and money problems involving fractions and decimals to two decimal places.	solve problems which require knowing percentage and decimal equivalents of $\frac{1}{2}$ , $\frac{1}{4}$ , $\frac{1}{5}$ , $\frac{2}{5}$ , $\frac{4}{5}$ and those with a denominator of a multiple of 10 or 25.			

## Fractions including Decimals and Percentages: Key Performance Indicators

Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
Recognise, find and name a half as one of two equal parts of an object, shape or quantity Recognise, find and name a quarter as one of four equal parts of an object, shape or quantity.	Recognise, find, name and write 1/3, 1/4, 1/2 and 3/4 of size, shape or quantity Write simple fraction facts, e.g. 1/2 of 6 = 3	Count up and down in tenths Understand that tenths are objectives or quantities divided into ten equal parts Compare and order simple fractions Recognise and show equivalent fractions Find and write fractions of a set of objects Add and subtract fractions with common denominators (less than one)	Recognise and use hundredths Recognise and write decimal equivalents to $\frac{1}{4}$ , $\frac{1}{2}$ and $\frac{3}{4}$ Divide one- or two-digit numbers by 10 and 100, using tenths and hundredths Round decimals with one decimal place to the nearest whole number Compare numbers up to two decimal places	Convert between mixed numbers and improper fractions Compare and order fractions whose denominators are multiples of the same number Identify, name and write equivalent fractions including tenths and hundredths Add and subtract fractions with denominators that are multiples of the same number Multiply proper fractions and mixed numbers by whole numbers with support Read and write decimal numbers as fractions Round decimals with 2 decimals places to whole number or to one decimal place Read, write, order and	Use common factors to simplify fractions Compare and order fractions of any size Add and subtract fractions with different denominators and mixed numbers Multiply simple pairs of proper fractions Divide proper fractions by whole numbers Calculate decimal fraction equivalents for simple fractions Multiply a number with up to two decimal places by whole numbers Use written division with answers of up to two decimal places Solve problems involving the calculation of percentages Recall and use equivalences

	compare numbers with up to	between fractions, decimals
	3 decimal places	and percentages
	Recognise % symbol and	
	explain as a fraction with	
	denominator 100 (parts out	
	of 100)	

## Fractions including Decimals and Percentages: Cross-curricular links

Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
DT - Cutting fruit in food technology to make a fruit kebab Art - Making fruit collages	DT - making cakes using half ingredient			identify, name and write equivalent fractions of a given fraction, represented visually, including tenths and hundredths (Vikings and Anglo Saxons - designing a shield).	

Fractions including	Decimals	and Percentages:	Vocabulary
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Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
Fraction	Fraction	Fractions	fraction	Fractions	fraction
Equal part	Equivalent fraction	Equivalent fraction	equivalent fraction	Proper fraction	proper/improper fraction
Equal grouping	Numerator	Numerator	mixed number	Improper fractions	equivalent fraction
Equal sharing	Denominator	Denominator	numerator	Equivalent fractions	mixed number
One of two equal parts	Egual part	Half	denominator	Mixed numbers	numerator
One of four equal parts	Equal grouping	Quarter	egual part	Numerator	denominator
	Equal sharing	One third	half	Denominator	eguivalent
	Parts of a whole	Two third	quarter	Equivalent	reduced to
	Half, two halves	Sixths/sevenths/eighths/tenths	third	Reduced to	proportion
	One of two equal parts	5	sixths	Cancel	in every
	Quarter, two three		sevenths	Parts of a whole	for every
	One of four equal parts		eighths	Thousandths	ratio
	One third		tenths	Decimal/decimal fractions	percentage
	Two third		hundredths	Decimal point	per cent
	One of three equal parts		decimal	Decimal place	%
			decimal fraction	Decimal equivalent	
			decimal point	Proportion	
			decimal place	Inevery	
			decimal equivalent	For every	
			'	Percentage	
				Per cent	
				%	